

**TDC Odd Semester Exam., 2020
held in July, 2021**

MATHEMATICS

(Honours)

(5th Semester)

Course No. : MTMH-502

(**Linear Programming**)

Full Marks : 50

Pass Marks : 17

Time : 2 hours

*The figures in the margin indicate full marks
for the questions*

Answer **five** questions, taking **one** from each Unit

UNIT—I

1. (a) Discuss the advantages and disadvantages of a model in OR. 5
- (b) Discuss the development of OR in India. 5

2. (a) Discuss assumptions of proportionality, additivity, continuity, certainty and finite choices in the context of linear programming. 5

- (b) Find the maximum value of
 $Z = 2x_1 + 3x_2$
subject to

$$\begin{aligned} x_1 + x_2 &= 30 \\ x_2 &\leq 3, x_2 \geq 12 \\ x_1, x_2 &\geq 0, 0 \leq x_1 \leq 20 \end{aligned}$$

UNIT—II

3. (a) Show that the convex combination of all feasible solutions to an LPP is again a feasible solution to the LPP. 5
- (b) Show that the intersection of two convex sets is also a convex set. 3
- (c) Show that a hyperplane is a convex set. 2
4. (a) Show that the set of all feasible solutions of an LPP is a convex set. 5
- (b) Show that a closed convex set which is bounded from below has extreme points on every supporting hyperplane. 5

(3)

UNIT—III

5. (a) What is the role of surplus variable in simplex method? 2
- (b) Write the steps involved in two-phase simplex method. 5
- (c) Explain the following with reference to LPP : 3
 Entering variable, leaving variable
6. (a) Use the Big M-method to
 Minimize $Z = 60x_1 + 80x_2$
 $x_1 \leq 400$
 $x_2 \leq 200$
 $x_1 + x_2 \leq 500$
 $x_1, x_2 \geq 0$ 5
- (b) Show that the LPP
 Maximize $Z = 2x_1 + 3x_2 + 4x_3 + x_4$
 subject to
 $x_1 + 5x_2 + 9x_3 + 6x_4 = 2$
 $3x_1 + x_2 + x_3 + 3x_4 = 10$
 $2x_1 + 3x_2 + 7x_3 + 8x_4 = 0$
 $x_1, x_2, x_3, x_4 \geq 0$
 has unbounded solution. 5

(4)

UNIT—IV

7. (a) Obtain the dual problem of the following LPP :
 Max $Z = 2x_1 + 5x_2 + 6x_3$
 subject to
 $5x_1 + 6x_2 + x_3 = 3$
 $2x_1 + x_2 + 4x_3 = 4$
 $x_1 + 5x_2 + 3x_3 = 1$
 $3x_1 + 3x_2 + 7x_3 = 6$
 $x_1, x_2, x_3 \geq 0$
- Also verify that the dual of the dual is primal itself. 5
- (b) Solve the LPP by duality theory
 Max $Z = 2x_1 + x_2 + 3x_3$
 subject to
 $x_1 + x_2 + 2x_3 = 5$
 $2x_1 + 3x_2 + 4x_3 = 12$
 $x_1, x_2, x_3 \geq 0$ 5
8. (a) Find the initial basic feasible solution to the following transportation problem by
 (i) minimum cost method
 (ii) north-west corner rule

(5)

State which of the methods is better.

	<i>To</i>			<i>Supply</i>
	2	7	4	5
	3	3	1	8
<i>From</i>	5	4	7	7
	1	6	2	14
<i>Demand</i>	7	9	18	6

(b) Prove that a necessary and a sufficient condition for the existence of a feasible solution to a transportation problem is that—

$$\text{total supply} = \text{total demand} \quad 2+2=4$$

UNIT—V

9. (a) Find the optimal assignment and the optimal cost from the following cost matrix : 7

	M_1	M_2	M_3	M_4
J_1	9	6	6	5
J_2	8	7	5	6
J_3	8	6	5	7
J_4	9	9	8	8

(b) Give a mathematical formulation of the assignment problem. 3

(6)

10. (a) Explain the difference between a transportation problem and an assignment problem. 4

(b) Discuss the steps of Hungarian method. 6
